# Increasing the location rate of Positron Emission Particle Tracking (PEPT) measurements 



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## Overview of PEPT



See Parker et al.; Nicușan and Windows-Yule

## Data generation



Figure 1: Siemens ECAT HR++ PET scanner at PEPT Cape Town.


Figure 2: GATE simulation of the HR++ PET camera as seen in Figure 2.

## The research problem

(a)

1. Simulation timestamps

Simulation times $=[0.00,0.11,0.33,0.82,1.01,1.25, \ldots] \mathrm{ms}$
2. Listmode timestamps

Millisecond times $=[0.00,0.00,0.00,0.00,1.00,1.00,1.00, \ldots] \mathrm{ms}$
3. Interpolated timestamps

Millisecond times $=[0.00,0.00,0.00,0.00,1.00,1.00,1.00, \ldots] \mathrm{ms}$


Interpolated times $=[0.00,0.25,0.50,0.70,1.00,1.25,1.50, \ldots] \mathrm{ms}$
(b)




Figure 3: Illustration (a) shows the interpolation algorithm and (b) shows the timestamps of the simulation, millisecond and interpolation LORs.

## Timestamp difference



Figure 4: The temporal error, $\Delta(t)$, for both the millisecond and the interpolated timestamps.

- The following fit results are for $\Delta(t)_{i, s}$
- $\mu=(-7.3 \pm 1.0) \times 10^{-4} \mathrm{~ms}, \beta=0.02014 \pm 0.00014 \mathrm{~ms}$
- Reduced $\chi^{2}=0.28, L=377 \pm 19 \mathrm{kHz}$


## Random walk model

- The $\gamma=0.0 \mathrm{~mm}, \sigma=1.0 \mathrm{~mm}$ and $\tau$ user defined.
- A moving average with a window size of 4 was applied.


Figure 5: The $X, Y$ and $Z$ dimensions of the random walk model for 0.5 s .

## Trajectory comparison

$\tau=0.1 \mathrm{~ms}$


Figure 6: $X$ dimension of path with $\tau=0.1 \mathrm{~ms}$


Figure 7: $X$ dimension of path with $\tau=1.0 \mathrm{~ms}$

## Velocity distributions



Figure 8: $v_{X}$ distributions for $\tau$ $=0.1 \mathrm{~ms}$.


Figure 9: $v_{X}$ distributions for $\tau$ $=1.0 \mathrm{~ms}$.

■ Large maximum $v_{X}$ for Figure 8 compared to Figure 9

## Trajectory uncertainties

Trajectory uncertainty equation

$$
\Delta(R)=\left[\sum_{j=0}^{n}\left|R_{i}(j)-R_{t}(j)\right|\right] / n
$$



Figure 10: The uncertainty, $\Delta(R)$, as a function of time step, $\tau$, for $\tau \in\{0.08,1.00\} \mathrm{ms}$.

## Similarity of velocity distributions

Jensen-Shannon distance (JSD)
A $J S D$ from 0 to 1 shows similarity to dissimilarity.


Figure 11: The $J S D$ as a function of time step, $\tau$, for $\tau \in\{0.08,1.00\} \mathrm{ms}$.

## Conclusion




■ $\uparrow$ in temporal resolution $\Rightarrow \uparrow$ in location frequency
■ $\downarrow$ of uncertainty in the trajectory

- This increases the ability of PEPT to track high speed tracers undergoing turbulent motion e.g. centrifuge pumps


## References

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## Thank you!

