Increasing the location rate of Positron Emission Particle Tracking (PEPT) measurements



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# Overview of PEPT



#### Data generation



Figure 1: Siemens ECAT HR++ PET scanner at PEPT Cape Town.



Figure 2: GATE simulation of the HR++ PET camera as seen in Figure 2.

See Perin et al.

#### The research problem



Figure 3: Illustration (a) shows the interpolation algorithm and (b) shows the timestamps of the simulation, millisecond and interpolation LORs.

See Hampel et al.

# Timestamp difference



Figure 4: The temporal error,  $\Delta(t)$ , for both the millisecond and the interpolated timestamps.

• The following fit results are for  $\Delta(t)_{i,s}$ 

•  $\mu = (-7.3 \pm 1.0) \times 10^{-4}$  ms,  $\beta = 0.02014 \pm 0.00014$  ms

Reduced  $\chi^2=$  0.28, L= 377  $\pm$  19 kHz

#### Random walk model

- The  $\gamma = 0.0$  mm,  $\sigma = 1.0$  mm and  $\tau$  user defined.
- A moving average with a window size of 4 was applied.



Figure 5: The X, Y and Z dimensions of the random walk model for 0.5 s .

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#### Trajectory comparison



Figure 6: X dimension of path with  $\tau = 0.1 \text{ ms}$ 

Figure 7: X dimension of path with  $\tau = 1.0 \text{ ms}$ 

# Velocity distributions



Figure 8:  $v_X$  distributions for  $\tau$  = 0.1 ms.

Figure 9:  $v_X$  distributions for  $\tau$  = 1.0 ms.

Large maximum  $v_X$  for Figure 8 compared to Figure 9

#### Trajectory uncertainties

Trajectory uncertainty equation

$$\Delta(R) = \left[\sum_{j=0}^{n} |R_i(j) - R_t(j)|\right] / n$$



Figure 10: The uncertainty,  $\Delta(R)$ , as a function of time step,  $\tau$ , for  $\tau \in \{0.08, 1.00\}$  ms.

# Similarity of velocity distributions Jensen-Shannon distance (JSD)

A JSD from 0 to 1 shows similarity to dissimilarity.



Figure 11: The JSD as a function of time step,  $\tau$ , for  $\tau \in \{0.08, 1.00\}$  ms.

# Conclusion



- $\uparrow$  in temporal resolution  $\Rightarrow \uparrow$  in location frequency
- $\blacksquare$   $\downarrow$  of uncertainty in the trajectory
- This increases the ability of PEPT to track high speed tracers undergoing turbulent motion *e.g.* centrifuge pumps

#### References

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#### Thank you!